

Unit #2: Rational Exponents and Complex Numbers.

Rational Equation $\frac{2}{x} = 3$

Variable in Denominator.

Rational Exponent - Exponents that
are fractions.

$16^{\frac{1}{4}}$ 16^2

Complex numbers - have a real and
an imaginary part.

$$i = \sqrt{-1}$$

$$2 + 3i$$

↑
real
↑
imaginary

Properties of exponents

$$a^m \cdot a^n = a^{m+n}$$

$$\text{ex } x^4 \cdot x^5 = x^9$$

$$2^3 \cdot 2^3 = 2^6 \quad (2 \cdot 2 \cdot 2)(2 \cdot 2 \cdot 2) = 2^6$$

$$\frac{a^m}{a^n} = a^{m-n} \quad \text{ex: } \frac{a^3}{a^2} = a^{3-2} = a^1 = a$$

$$(a^m)^n = a^{m \cdot n} \quad \text{ex } (5^3)^4 = 5^{12}$$

$$(ab)^m = a^m b^m \quad \text{ex } (2xy)^4 = 2^4 x^4 y^4 = 16x^4 y^4$$

$$a^{-n} = \frac{1}{a^n} \quad \text{ex } 2^{-4} = \frac{1}{2^4}$$

$$\frac{1}{3^{-2}} = 3^2$$

$$x^{-2} y^3 = \frac{y^3}{x^2}$$

$$X^{\frac{1}{2}} = \sqrt{X}$$

↑ Radical Form

Exponent
Form

$$4^{\frac{1}{2}} = \sqrt{4}$$

$$4^{\frac{1}{2}} = 2$$

$$8^{\frac{1}{3}} = \sqrt[3]{8} = 2$$

← cube root

$$27^{\frac{1}{3}} = \sqrt[3]{27} = 3$$

$$\sqrt[4]{15} = 15^{\frac{1}{4}}$$

$$7^{\frac{1}{2}} \cdot 7^{\frac{1}{2}} = \sqrt{7} \cdot \sqrt{7}$$

$$\downarrow = \sqrt{7 \cdot 7}$$

$$7^{\frac{1}{2} + \frac{1}{2}} = \sqrt{49}$$

$$\downarrow = 7$$

$$\begin{aligned}\underline{5^{\frac{1}{4}} \cdot 125^{\frac{1}{4}}} &= \sqrt[4]{5} \cdot \sqrt[4]{125} \\ &= \sqrt[4]{5 \cdot 125} \\ &= \sqrt[4]{625} \\ &= 5\end{aligned}$$

$$6^{\frac{2}{3}} = \sqrt[3]{6^2}$$

(write in Radical Form)

$$x^{\frac{2}{3}} = \sqrt[3]{x^2}$$

$$2^{\frac{3}{5}} = \sqrt[5]{2^3}$$

write in exponential Form

Using a calculator to find

$$\sqrt[4]{625}$$

4 2nd $\frac{\square}{\square}$ 625 = 5

^

$$\sqrt{16} = 4$$

$\sqrt{\square}$

x^2

$$P = d^{\frac{3}{2}}$$

↑
distance in AU

$$= 1.52^{\frac{3}{2}}$$

$$= \sqrt[2]{1.52^3}$$

$$= \sqrt[2]{3.51}$$

$$= 1.87$$

$$P = 0.72^{\frac{3}{2}}$$

$$= \sqrt[2]{0.72^3} = 0.37$$

